# Solubility and Diffusivity of Sulfur Dioxide in Latex Paint Films

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### **Synopsis**

Sorption of  $SO_2$  in latex paint films is measured as a function of time. This data is used to extract the solubility (S) and the diffusion coefficient (D) for  $SO_2$  in these films. The solubility of  $SO_2$  in each of the samples follows Henry's law behavior. Sorption occurs only in the polymer, with the inorganic pigment particles acting as impenetrable fillers. The diffusion of  $SO_2$  is Fickian with an exponential dependence upon the concentration of  $SO_2$ . This data is used to calculate the permeabilities of the paint samples to  $SO_2$ , at levels typically found in the atmosphere.

## **INTRODUCTION**

Over the last decade the problem of acid rain has grown from being the concern of small environmental groups to its present status near the top of governmental priorities. This acidified precipitation poses serious threats to the world's forest reserves and structural materials. In many cases the only protection offered to these structural materials comes from a few mils of paint. Paints protect a substrate, usually of wood or metal, by forming a barrier to harmful gases and vapors present in the environment. With the increasing tenacity of the attacking species in the atmosphere (such as SO<sub>2</sub> and NO<sub>x</sub> gases from automobile emissions) questions are being raised about how successfully these paints are performing.<sup>1-4</sup>

In assessing the possible deleterious effects of pollutant gases on paint films, it is of use to know how much gas dissolves in the paint film and how rapidly it moves through the paint film. The physical quantities of interest are the solubility (S), the diffusivity (D), and the permeability (P). For polymers above their glass transition temperature  $(T_g)$ , solubility follows Henry's law,

$$C = Sp \tag{1}$$

where C represents concentration of dissolved species in equilibrium with a gas of partial pressure p. Diffusion in thin polymer films above their  $T_g$  along the thickness direction (x) generally follows Fick's law,

$$J = -D \frac{\partial C}{\partial x} \tag{2}$$

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where J is the flux of penetrant through the film subject to a concentration gradient of  $\partial C/\partial x$  and D represents the (concentration-independent) diffusion coefficient. These two quantities S and D can be deduced by measuring the mass of gas sorbed by a thin film of paint as a function of time.<sup>5-13</sup> The permeability is defined as the product of S and D.

Many investigations of SO<sub>2</sub> solubility, diffusivity, and permeability in polymeric materials have been undertaken. Felder, Spence, and Ferrell have compiled some of the findings.<sup>14</sup> Typical values for SO<sub>2</sub> permeability at 25°C are  $1.32 \times 10^{-9}$  and  $4.32 \times 10^{-8}$  (cm<sup>2</sup> cc SO<sub>2</sub> (STP)/cc sample cm Hg s) in poly (vinyl chloride) and poly (methyl methacrylate), respectively. Funke and Haagen<sup>15</sup> report SO<sub>2</sub> as having a high diffusivity in many polymeric coatings for a molecule of its size. Keuhe and Friedlander<sup>16</sup> found the solubility of SO<sub>2</sub> in polyacrylate to be very high. Davis and co-workers report high permeabilities for SO<sub>2</sub> in other commercial polymers<sup>17,18</sup> such as  $2.09 \times 10^{-9}$  (same units as above) for polyethylene;  $6.58 \times 10^{-10}$  for polyamide;  $2.24 \times 10^{-9}$  for polycarbonate and  $2.01 \times 10^{-11}$  for the copolymer of vinylidene chloride and vinyl chloride.

Latex paints are composed of a latex base polymer with various additive extenders, emulsifiers, pigments, fungicides, and others. These paint additives may aid or hinder the solubility and diffusivity of an atmospheric component in the paint. Relatively little work regarding solubilities and diffusivities of pollutant gases in latex paints has appeared in the literature. In this work gravimetric determinations are made of the solubility and diffusivity of SO<sub>2</sub> in two latex paint formulas, and in the base polymer common to both.

#### EXPERIMENTAL

**Samples.** Two exterior grade latex paint formulations were prepared by and obtained from Union Carbide Coatings and Emulsions (Cary, NC). The base polymer, common to both paints, was also supplied. This latex was reported to be copolymer containing a 1:1:1 mole ratio of vinyl chloride, vinyl acetate, and butyl acrylate, with small amounts (less than 7 mol %, total) of methyl acrylate, methyl methacrylate, and acrylic acid. The two paints differed in that one contains a CaCO<sub>3</sub> extender while the other includes no CaCO<sub>3</sub>. The paint compositions are listed in Table I, and the approximate dry film compositions are listed in Table II. The values in Table II were obtained by assuming that all volatile paint components are removed in the drying process.

Density measurements of the three samples were carried out using an Archimedes apparatus and are as follows:  $1.287 \text{ g/cm}^3$  for the base latex;  $2.112 \text{ g/cm}^3$  for the latex with CaCO<sub>3</sub>; and  $2.122 \text{ g/cm}^3$  for the latex without CaCO<sub>3</sub>.

**Paint Film Preparation.** Films of uniform thickness were prepared from the samples by casting with a draw bar on clean glass plates. The films remained on the plates in a dust-free environment under room conditions for 16 h. The samples were then placed in a freezer for 3–6 h and removed to room temperature for 10 min in order to aid in removing the films from the glass plates. The films were then stored in a desiccator over anhydrous CaSO<sub>4</sub> for a minimum of 3 days. Determination of film thickness was achieved through the use of a micrometer having a precision of  $\pm 1.2 \ \mu$ m. Film thickness for this study was on the order of 5 mils (127  $\mu$ m).

	Wt %		
Components	Latex w/CaCO <sub>3</sub>	Latex w/o CaCO <sub>3</sub>	
Water	20.5	20.5	
UCAR 516 (acrylic terpolymer)	35.0	35.0	
RCL 9 TiO <sub>2</sub> (pigment)	21.2	25.4	
Genstar camel white (CaCO <sub>3</sub> extender)	12.7	0.0	
Optiwhite P (china clay extender)	4.2	12.7	
Aqualon $H_4Br$ (bioresistant thickener)	0.2	0.2	
BYK 155 (dispersant)	0.8	0.8	
TKPP (codispersant)	0.1	0.1	
Triton N101 (nonionic surfactant)	0.2	0.2	
Nalco 2315 (foam reduction)	0.3	0.3	
Ethylene glycol	2.4	2.4	
Texanol (coalescent)	1.4	1.4	
Trysan polyphase (biocide)	0.8	0.8	
Ammonium hydroxide	0.2	0.2	

TABLE I Acrylic Latex Paint Composition

**Sorption–Desorption Measurements.** A McBain<sup>13</sup> balance with quartz springs (spring constants = 0.51 and 0.332 mg/mm) were used to perform mass uptake measurements of SO<sub>2</sub> as a function of time. The deflection of the sample suspended on the end of the spring was recorded through the use of an optical reader traveling vertically on a calibrated shaft (cathetometer). The ultimate sensitivity of this system is 0.026 mg and 0.017 mg for the two springs mentioned above. Anhydrous grade SO<sub>2</sub> was purchased from Union Carbide and was reported to be 99.98% pure. This gas was used as received and the system pressures reported are as read from a mercury manometer with a readability of  $\pm 1$  mm. A mechanical vacuum pump was used to evacuate the system and degas the sample; it could achieve vacuum of 1 mtorr. Temperature control was maintained to  $\pm 1^{\circ}$ C by circulating water through a jacket surrounding the sorption cell.

# **RESULTS AND DISCUSSION**

The treatment of the sorption (or desorption) data is represented in Figure 1, where  $M_t$  is the mass of SO<sub>2</sub> sorbed (or desorbed) at time t and  $M_{\infty}$  is the

TABLE II Approximate Dry Film Composition					
	Latex paint (w/CaCO <sub>3</sub> )		Latex paint (w/o CaCO <sub>3</sub> )		
Component	(wt %)	(vol %)	(wt %)	(vol %)	
Latex base polymer	37	61.6	37	63.6	
CaCO <sub>3</sub>	21	16.1	0	0.0	
$TiO_2$	35	17.6	42	22.0	
China clay	7	4.7	21	14.4	



Fig. 1. A typical plot showing the treatment of the sorption and desorption data. The data shown is for the base polymer at 28°C and 161 torr of  $SO_2$ .

mass of  $SO_2$  sorbed (or desorbed) at equilibrium. The data is plotted for convenient use of

$$\frac{M_{\rm t}}{M_{\infty}} = \frac{4}{l} \left( \frac{Dt}{\pi} \right)^{0.5} \tag{3}$$

which describes Fickian diffusion in a thin film at short times. In eq. (3), l represents the film thickness while D is the diffusion coefficient. The slope of the initial linear region from plots such as Figure 1 is used with eq. (3) to determine D.

Sorption isotherms are obtained by plotting  $M_{\infty}$  vs. pressure. Sorption isotherms acquired at 28°C for SO<sub>2</sub> in the two paint samples and the base polymer are displayed in Figure 2. All samples exhibit the expected Henry's law behavior for a polymer above its  $T_g$ . In accordance with previous work with SO<sub>2</sub> in other polymers,<sup>14</sup> the solubility is quite high; the polymer base absorbs about 13% by weight at 1 atm of SO<sub>2</sub>. The isotherms nearly superimpose when the amount of SO<sub>2</sub> sorbed by the paint samples is normalized to the amount of polymer in the paint (37%, from Table II). This is shown by the dashed lines in Figure 2, and indicates that sorption occurs only in the polymer, with the inorganic additives in the paint samples acting simply as impenetrable fillers. The small differences in the normalized isotherms for the three samples could be due to the uncertainty in the amount of polymer contained in each paint. Adjustments to this number of less than 4% will cause the isotherms for all three samples to superimpose perfectly. The solubilities are listed in Table III for these isotherms isotherms for the set of the set.



Fig. 2. Isotherms for several paint samples taken at  $28^{\circ}$ C: (----) least-squares fit to data; (---) isotherms for the paint samples normalized to the mass of polymer base contained in each sample using a factor of 0.37 g polymer base/g sample.

therms (run 2), as well as for a second set of samples (run 1) to illustrate the degree of reproducibility. In the worst case (latex without  $CaCO_3$ ), the solubilities from the two runs differ by about 11%. Also listed in Table III are the unnormalized solubilities for the paints, in terms of grams of sample.

The diffusion coefficient was calculated from plots such as Figure 1 at each pressure, and was found to be pressure (concentration)-dependent. This is not surprising for high-solubility penetrants (such as  $SO_2$ ) that are likely to plasticize the polymer. In cases where D is concentration-dependent, an average diffusion coefficient  $D_{ave}$  is usually defined, which describes transport over some small concentration range  $C_1-C_2$ :

$$D_{\text{ave}} = \frac{1}{C_2 - C_1} \int_{C_1}^{C_2} D(C) \, dc \tag{4}$$

Sample	$S (mg SO_2/g sample torr)$		$S (mg SO_2/g polymer torr)$			
	Run #1	Run #2	Run #1	Run #2		
Latex base	0.192	0.186	0.192	0.186		
Latex w/o CaCO <sub>3</sub>	0.0720	0.0641	0.194	0.173		
Latex w/ CaCO <sub>3</sub>	0.0620	0.0623	0.168	0.168		

 TABLE III

 Solubilities (S) for Sulfur Dioxide in Paint Samples

An approximation to  $D_{ave}$  is obtained by performing integral sorption and desorption experiments at each pressure, calculating the sorption and desorption diffusion coefficients from eq. (3) and averaging these two numbers. In integral sorption  $C_1 = 0$  for sorption and  $C_2 = 0$  for desorption.

For Fickian diffusion in polymers above  $T_g$ , for which the sorbed penetrant concentration does not exceed approximately 10 wt % of polymer, an exponential dependence of D on concentration is common, i.e.,

$$D_{\text{ave}} = D_0 \exp(AC) \tag{5}$$

Here  $D_0$  is the penetrant diffusivity at infinite dilution, and A is a "plasticization parameter."<sup>20-24</sup> A plot of  $\ln D_{ave}$  as a function of pressure is presented in Figure 3. The fit to the data for the latex base is reasonably good, while the data for the paints show considerably more scatter. The values of  $D_{ave}$  for the base polymer are consistently higher than for the two paint samples, which seem to have the same  $D_{ave}$  at a given pressure. This is as expected since the diffusing molecules are not hindered in their motion through the polymer network by the presence of the filler particles in the base latex while these obstacles are present in the two paints. The lower values for the diffusion coefficient in the two paints is very likely due to the increase in the diffusion path for a penetrant molecule which must travel around these filler particles.

In spite of the scatter in the data for the paints, the slope of all three lines in Figure 3 are essentially equal, indicating that the polymer phase in each



Fig. 3. A semilog plot of the average diffusion coefficients for the three samples against  $SO_2$  pressure. The lines are least-square fits to the data, showing an exponential dependence of the diffusion coefficients on pressure.

sample undergoes the same amount of plasticization when the concentration of  $SO_2$  in the polymer phase is the same (i.e., at equal pressures). However, the overall concentration of  $SO_2$  in the paints (per gram sample) is less than it is in the base polymer for a given pressure, as shown in Figure 1. This leads to higher diffusivities in the paint samples when the data is plotted versus concentration instead of pressure (except when C approaches 0). The net effect is to make the paint samples appear more plasticizable than the unfilled base polymer. This is manifested in the plasticization parameter A, which has been calculated from the slopes in Figure 3 and

$$\ln(D_{ave}) = \ln(D_0) + ASp \tag{6}$$

where C in eq. (5) has been replaced by Sp. The values of S used to obtain A were the two-run averages of the unnormalized solubilities (per gram sample) from Table III. The results are listed in Table IV, along with values for  $D_0$ .

Permeability is defined as the product of the solubility and the diffusivity. Predicted permeabilities based on the diffusivities in Figure 3 and the average unnormalized solubilities (per gram sample) from Table III are plotted against pressure in Figure 4. Standard units for permeability have been used. The permeability curves follow the same trends with pressure as the diffusivity; semilog plots yield reasonably good straight lines. It should be emphasized that experiments designed to directly measure permeability from the steady-state flux of penetrant through the samples may not produce the same values as obtained here. This is due to the fact that the diffusion coefficient D is concentration-dependent, and experiments designed to directly measure P produce a constant concentration gradient across the sample. Therefore, permeability varies throughout the sample, and the value obtained is an integral average of the concentration-dependent permeability across the thickness of the sample. In our experiments for measuring D, a concentration gradient exists at the beginning of the experiment, but eventually disappears as the sorption of penetrant approaches its equilibrium value. Thus, D varies not only with position in the sample, but with time as well. The boundary conditions are clearly different for the two types of experiments, and results for the pressure dependence of the permeability cannot be directly translated from one to the other.

In any case, the permeability in the infinite dilution regime, where concentration dependence vanishes, should be comparable for both types of experiments. This quantity,  $P_0 = D_0 S$ , has been listed in the last column of Table IV. Maximum atmospheric levels of SO<sub>2</sub> seldom exceed 10 ppb (7.6  $\times$  10<sup>-6</sup> torr), so that these  $P_0$  values should produce reasonable practical estimates of

Zero-Pressure Diffusivities and Permeabilities of $SO_2$				
Sample	A (g sample/mg SO <sub>2</sub> )	D <sub>0</sub> (cm <sup>2</sup> /s)	$P_0$ (cm <sup>2</sup> cc SO <sub>2</sub> (STP)/ cc sample cm Hg s)	
Latex base	0.0135	$1.42 imes10^{-8}$	$1.21 imes 10^{-8}$	
Latex w/o CaCO <sub>3</sub>	0.0366	$1.09 imes10^{-8}$	$5.52 imes10^{-9}$	
Latex w/ CaCO <sub>3</sub>	0.0420	$1.06 imes10^{-8}$	$4.88 imes10^{-9}$	



Fig. 4. Calculated permeabilities for the three samples using diffusivities from Figure 3 and average solubilities from Table III. The lines are least-square fits to the data.

the atmospheric SO<sub>2</sub> flux through these paint films at 28°C. Comparison of the S, D, and P values reported here with values for other polymers is hard to make since very little work with acrylic latex films has been reported; however, comparisons of SO<sub>2</sub> solubilities, diffusivities, and permeabilities in other amorphous polymers of similar  $T_g$  ( $\approx 10^{\circ}$ C) show good agreement.<sup>14</sup>

## CONCLUSIONS

Sorption and diffusivity measurements for SO<sub>2</sub> in representative acrylic latex paints and the base polymer at 28°C have indicated that SO<sub>2</sub> is very soluble in the base polymer. The presence of impenetrable inorganic additive particles in the paints lowers the effective solubility of SO<sub>2</sub> in these samples proportionately. Henry's law describes the sorption process in all three samples over a pressure range of 50–700 torr. The diffusivity decreases exponentially with decreasing pressure (concentration) over this pressure range, falling to within 5% of its limiting (infinite dilution) value at about 20 torr. At a given pressure, the diffusivity of SO<sub>2</sub> in the base polymer is slightly higher than in the paints, due to the presence of additive particles in the paints. The limiting permeabilities expected to be applicable at typical atmospheric levels of SO<sub>2</sub> (< 10 ppb) are calculated to be  $1.21 \times 10^{-8}$ ,  $5.52 \times 10^{-9}$ , and  $4.88 \times 10^{-9}$  cm<sup>2</sup> cc SO<sub>2</sub> (STP)/ cc sample cm Hg s, for the polymer base, the latex without CaCO<sub>3</sub>, and the latex with CaCO<sub>3</sub>, respectively. The authors gratefully acknowledge the support of this work by the U.S. Environmental Protection Agency through Cooperative Agreement #CR-814166-01-0.

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